## Core Mathematics C1 Paper E

1. (i) Express $\frac{21}{\sqrt{7}}$ in the form $k \sqrt{7}$.
(ii) Express $8^{-\frac{1}{3}}$ as an exact fraction in its simplest form.
2. Find $\frac{\mathrm{d} y}{\mathrm{~d} x}$ when
(i) $y=x-2 x^{2}$,
(ii) $y=\frac{3}{x^{2}}$.
3. (a) Express $x^{2}-10 x+27$ in the form $(x+p)^{2}+q$.
(b) Sketch the curve with equation $y=x^{2}-10 x+27$, showing on your sketch
(i) the coordinates of the vertex of the curve,
(ii) the coordinates of any points where the curve meets the coordinate axes.
4. The straight line $l_{1}$ has gradient 2 and passes through the point with coordinates $(4,-5)$.
(i) Find an equation for $l_{1}$ in the form $y=m x+c$.

The straight line $l_{2}$ is perpendicular to the line with equation $3 x-y=4$ and passes through the point with coordinates $(3,0)$.
(ii) Find an equation for $l_{2}$.
(iii) Find the coordinates of the point where $l_{1}$ and $l_{2}$ intersect.
5. Given that the equation

$$
4 x^{2}-k x+k-3=0,
$$

where $k$ is a constant, has real roots,
(i) show that

$$
\begin{equation*}
k^{2}-16 k+48 \geq 0 \tag{2}
\end{equation*}
$$

(ii) find the set of possible values of $k$,
(iii) state the smallest value of $k$ for which the roots are equal and solve the equation when $k$ takes this value.
6. The points $P$ and $Q$ have coordinates $(-2,6)$ and $(4,-1)$ respectively.

Given that $P Q$ is a diameter of circle $C$,
(i) find the coordinates of the centre of $C$,
(ii) show that $C$ has the equation

$$
\begin{equation*}
x^{2}+y^{2}-2 x-5 y-14=0 \tag{5}
\end{equation*}
$$

The point $R$ has coordinates $(2,7)$.
(iii) Show that $R$ lies on $C$ and hence, state the size of $\angle P R Q$ in degrees.
7. (i) Describe fully the single transformation that maps the graph of $y=\mathrm{f}(x)$ onto the graph of $y=\mathrm{f}(x-1)$.
(ii) Showing the coordinates of any points of intersection with the coordinate axes and the equations of any asymptotes, sketch the graph of $y=\frac{1}{x-1}$.
(iii) Find the $x$-coordinates of any points where the graph of $y=\frac{1}{x-1}$ intersects the graph of $y=2+\frac{1}{x}$. Give your answers in the form $a+b \sqrt{3}$, where $a$ and $b$ are rational.
8.


The diagram shows the curve $C$ with the equation $y=x^{3}+3 x^{2}-4 x$ and the straight line $l$.

The curve $C$ crosses the $x$-axis at the origin, $O$, and at the points $A$ and $B$.
(i) Find the coordinates of $A$ and $B$.

The line $l$ is the tangent to $C$ at $O$.
(ii) Find an equation for $l$.
(iii) Find the coordinates of the point where $l$ intersects $C$ again.
9. The curve with equation $y=2 x^{\frac{3}{2}}-8 x^{\frac{1}{2}}$ has a minimum at the point $A$.
(i) Find $\frac{\mathrm{d} y}{\mathrm{~d} x}$.
(ii) Find the $x$-coordinate of $A$.

The point $B$ on the curve has $x$-coordinate 2 .
(iii) Find an equation for the tangent to the curve at $B$ in the form $y=m x+c$.

